

COMBINATORICS  
SEMINAR

*Cleaning  $d$ -regular graphs with brushes*

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**Abstract:** A model for cleaning a graph with brushes was recently introduced. We consider the minimum number of brushes needed to clean  $d$ -regular graphs in this model, focusing on the asymptotic number for random  $d$ -regular graphs. We use a degree-greedy algorithm to clean a random  $d$ -regular graph on  $n$  vertices (with  $dn$  even) and analyze it using the differential equations method to find the (asymptotic) number of brushes needed to clean a random  $d$ -regular graph using this algorithm (for fixed  $d$ ). We further show that for any  $d$ -regular graph on  $n$  vertices at most  $n(d+1)/4$  brushes suffice, and prove that for fixed large  $d$ , the minimum number of brushes needed to clean a random  $d$ -regular graph on  $n$  vertices is asymptotically almost surely  $n(d+o(d))/4$ .

(Joint work with Noga Alon and Nick Wormald.)

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