Let $A \subseteq \mathbb{R}^n$ be open and connected. Assume that $f : A \rightarrow \mathbb{R}$ is differentiable in $A$, with partial derivatives $\frac{\partial f}{\partial x_i} = 0$ for $i = 1, \ldots, n$. Show that $f$ is constant.