Consensus List Colorings of Graphs

Fred S. Roberts  
Rutgers University  
Piscataway, NJ, USA

Abstract

In graph coloring, one assigns a color to each vertex of a graph so that neighboring vertices get different colors. We shall talk about a consensus problem relating to graph coloring and discuss a variety of applications arising from traffic phasing, channel assignment, scheduling, routing, fleet maintenance, and DNA physical mapping. In many applications of graph coloring, one gathers data about the acceptable colors at each vertex. A list coloring is a graph coloring so that the color assigned to each vertex belongs to the list of acceptable colors associated with that vertex. We consider the situation where a list coloring cannot be found. If the data contained in the lists associated with each vertex are made available to individuals associated with the vertices, it is possible that the individuals can modify their lists through trades or exchanges until the group of individuals reaches a set of lists for which a list coloring exists. We describe several models under which such a consensus set of lists might be attained and connect them to the applications of interest.